

## MATH 1A – QUIZ 8

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Name: \_\_\_\_\_

**Instructions:** You have 20 minutes to take this quiz, for a total of 10 points. May your luck be concave up!

(1) (4 points; 1 point each) Let  $f(x) = x^5 - 5x^4$

- (a) Find the intervals of increase/decrease
- (b) Find the points at which  $f$  attains a local maximum/minimum
- (c) Find the intervals of concavity and the  $x$ -coordinates of the inflection points
- (d) Sketch a rough graph of  $f$

(2) (3 points; 1.5 points each) Evaluate the following limits:

(a)  $\lim_{x \rightarrow 0^+} x (\ln(x))^2$

(b)  $\lim_{x \rightarrow \infty} \left(1 + \frac{a}{x}\right)^{bx}$  (here  $a$  and  $b$  are constants)

(3) (3 points) We say that  $x$  is a **fixed point** of  $f$  if  $f(x) = x$

(for example,  $-1$  is a fixed point of  $x^3$  because  $(-1)^3 = -1$ )

Show that if  $f'(x) \neq 1$  for all  $x$ , then  $f$  has at most one fixed point.

**Note:** Fixed points are really cool! There's a famous fixed point theorem that states that if you shake a snowglobe, there will always be one snowflake that ends up at the same spot it started with. :)